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# Hydraulic Diagrams

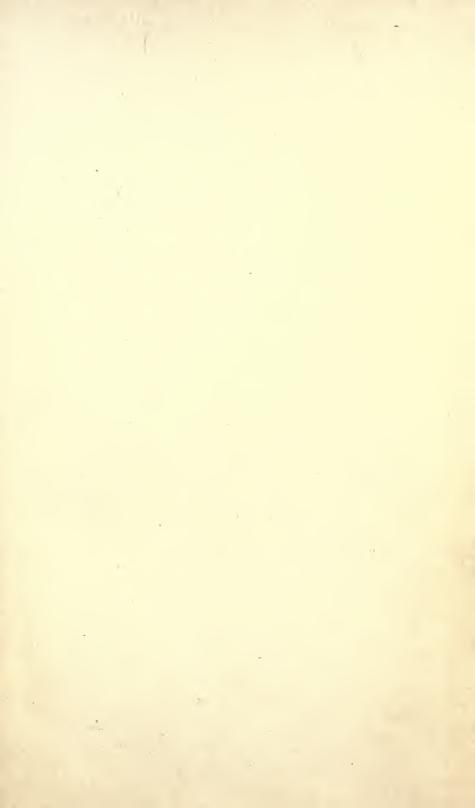
SWAN AND HORTON

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### HYDRAULIC DIAGRAMS

FOR THE

# DISCHARGE OF CONDUITS AND CANALS

Based upon the Formula of Ganguillet and Kutter

 $\mathbf{B}\mathbf{Y}$ 

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WITH

A Description of the Diagrams and their Use by Theodore Horton



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## PREFACE TO SECOND EDITION.

The following set of diagrams, based upon the formula of Ganguillet and Kutter, is intended for use in the study of such sections of conduits and canals as are commonly employed in sewerage, water supply, water power and land drainage. The set includes conduits of eight different types of cross-section, and canals of rectangular and trapezoidal cross-section.

In presenting this set of diagrams, it has been the aim of the authors to cover the field with as limited a number of diagrams as will readily conform to a simple and practical system for use. A short discussion of the formula and a description of the diagrams and their use appear on the following pages.

In this edition one diagram has been added to the set. This diagram, No. 1, gives discharges and velocities for the smaller diameters of conduits on a scale much larger than was used on diagram No. 1 of the previous edition. No changes have been made in the text other than italicizing certain phrases for the purpose of emphasis.

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#### DIAGRAMS.

#### (Following text.)

## DISCHARGE FROM CIRCULAR CONDUITS FLOWING FULL WITH N=0.015.

- I. Diameters of 3 ins. to I ft. 6 ins. and Hydraulic Inclinations of 0.10 to 0.0001.
- 2. Diameters of 4 ins. to 4 ft. and Hydraulic Inclinations of 0.10 to 0.0001.
- 3. Diameters of 6 ins. to 10 ft. and Hydraulic Inclinations of 0.006 to 0.000025.
- 4. Diameters of  $4\frac{1}{2}$  to 20 ft. and Hydraulic Inclinations of 0.0055 to 0.000025.
- 5. Ratios of Discharge for Different Values of n to Discharge for n = 0.015, for Circular Sections.

### RATIOS OF HYDRAULIC ELEMENTS OF VARIOUS SECTIONS.

- 6. Circular Section.
- 7. Gothic Section.
- 8. Basket Handle Section.
- 9. Catenary Section.
- 10. Egg-Shaped Section.
- 11. Square Section.
- 12. Horseshoe Section (Wachusett Aqueduct).
- 13. Horseshoe Section (Croton Aqueduct).
- 14. Discharge from Rectangular Filled Sections, n = 0.025.
- 15. Ratios of Discharge for Different Values of n to Discharge for n = 0.025, for Rectangular and Trapezoidal Sections.
- Ratio of Discharge of Filled Segment to that of Filled Section.
- 17. Ratio of Area of Segment to Area of Filled Section.

### HYDRAULIC DIAGRAMS FOR THE DISCHARGE OF CONDUITS AND CANALS.

#### CHAPTER I.

The Formula of Ganguillet and Kutter.

This formula for the mean velocity of discharge of rivers, canals and conduits was obtained from a comparison of numerous experiments made in different countries upon natural and artificial water courses of many sizes and various kinds of materials.

The formula assumes that a uniform flow has been established and gives the equation of the mean velocity of flow. This equation is as follows for metric measures:

$$V = \left\{ \frac{23 + \frac{I}{n} + \frac{0.00155}{S}}{I + (23 + \frac{0.00155}{S}) \frac{n}{\sqrt{R}}} \right\} \sqrt{\frac{R}{S}}$$

When reduced to measures in English feet it becomes

$$V = \begin{cases} \frac{41.6603 + \frac{1.81132}{n} + \frac{0.00281}{S}}{1 + (41.6603 + \frac{0.00281}{S}) \frac{n}{\sqrt{R}}} \end{cases} \sqrt{RS}$$

It may be expressed more briefly,

$$V = c \sqrt{R S}$$

in which

V= the mean velocity of flow;

c = the velocity coefficient;

R= the mean hydraulic radius of the stream;

 $S \leq$  the sine of the inclination, or fall in a unit of length;

n = a frictional factor dependent upon the nature of the surface over which the water flows.

For brevity, let us substitute letters for the numbers in the formula. We may then write

$$V = \left\{ \frac{a + \frac{1}{n} + \frac{m}{S}}{1 + (a + \frac{m}{S}) \frac{n}{\sqrt{R}}} \right\} \sqrt{RS}$$

and by substituting  $x = (a + \frac{m}{S})$  n and  $z = a + \frac{1}{n} + \frac{m}{S}$  we may

write

$$V = \left\{ \frac{z}{1 + \frac{x}{\sqrt{R}}} \right\} \sqrt{RS}$$

in which

$$c = \frac{z}{1 + \frac{x}{\sqrt{R}}}$$

When the quantity V is sought from general data, and the coefficient c is not needed separately, the following transformation may be made:

$$V = \left\{ \frac{z\sqrt{S}}{\sqrt{R} + x} \right\} R$$

which is a useful form from which tables may be calculated, and, as was done with many of the present diagrams, the results plotted.

Since a proper selection of the friction factor n is essential in the application of the above general equation and the use of the present diagrams based thereon, the following values for it will be here reproduced for a general guide in practice:

- n = .007 to .008: Glass, new tin, lead and galvanized iron pipe.
- n = .008 to .009: New seamless wrought-iron and new-coated cast-iron pipe in best of condition and alinement.
- n = .009 to .010: New cast-iron pipe, new enamelled and glazed pipe of all sorts; well planed timber in perfect alinement.
- n = .010 to .011: New wrought-iron riveted pipe of small diameter; new wooden stave pipe; planed timber, neat cement.
- n = .011 to .012: Unplaned timber carefully joined; cement, one-third sand; new terra cotta; new well-laid brickwork, carefully pointed and scraped; clean cast-iron pipe in use some time.
- n = .012 to .013: Unplaned timber; cement two-thirds sand; ashlar and well-laid brickwork; ordinary brickwork plastered; earthen and stoneware pipes in good condition but not new; plaster and planed wood of inferior quality; glazed pipe poorly laid or foul from use; new wrought-iron riveted pipe with many joints and rivets.
- n = .015: Rough-faced brickwork; ashlar and well-laid brickwork slightly deteriorated from use; fouled or slightly tuberculated cast-iron pipe; large wrought-iron riveted pipe, few years in use but in good condition; canvas lining.
- n = .017: Brickwork and ashlar in inferior condition or badly fouled; tuberculated and fouled iron pipe; rubble in cement or plaster, in good condition; gravellined canals with \(^3\_8\)-in. grains well rammed or cement grouted.
- n = .020: Rubble in cement of inferior quality; coarse rubble set dry; brickwork in bad condition; gravel-lined canals, with one-inch grains, well rammed or cement grouted.
- n = .0225: Rough rubble in bad condition; canals with earthen beds in perfect order and alinement.

- n = .025: Canals with earthen beds in good order and alinement and free from stones and weeds.
- n = .030: Canals with earthen beds in moderately good order and alinement, with few stones and weeds.
- n = .040: Canals with earthen beds in bad condition and alinement, having stones and weeds in great quantity.

For a more complete statement of the formula and its derivation the reader is referred to the following well-known books:

"The New Formula for Mean Velocity of Discharge of Rivers and Canals." By W. R. Kutter. Translated from Articles in the Cultur-Ingenieur by Louis D'A. Jackson. London, 1876.

"Flow of Water in Rivers and other Channels." By Ganguillet and Kutter. Translated, with numerous additions, by R. Hering and J. C. Trautwine. New York, 1891."

#### CHAPTER II.

#### Description of the Diagrams.

For convenience in their description, the diagrams will be considered under the following two groups: The first group, Diagrams I to I3, inclusive, deal with circular and similar types of conduits, more especially applicable to the conveyance of moderate volumes of water and sewage, flowing either openly or under pressure. The second group, Diagrams I4 to I7, inclusive, deal with canals of rectangular and trapezoidal cross sections, more applicable to the conveyance of larger volumes of water and sewage, not flowing under pressure.

#### Conduits.

Diagrams 1—4: Of the first group, Diagrams 1, 2, 3 and 4 are discharge diagrams, very similar in construction, and, differing only in range of data, will be described together. They give velocities in feet per second, and discharges in cubic feet per second, from circular conduits, running full, for diameters ranging from 3 ins. to 20 ft.; hydraulic inclinations from 0.000025 to 0.10; with a friction factor n = .015.

The vertical scale on each diagram represents hydraulic inclina-

tions, expressed fractionally at the right and trigonometrically (i. e. the sine of the angle of inclination) at the left. Also, at the left is given a scale of corresponding square roots of the slope. The horizontal scale represents discharges in cubic feet per second. Beginning at the left on Diagrams 3 and 4 this scale is broken at intervals, and at the same time increased in value, thus giving the diagrams a wider range of data than could be obtained by the use of a single scale. The radial lines represent diameters in feet and fractions thereof. By selecting a natural vertical scale, based upon the square root of the slope, these lines become straight between successive divisions of the horizontal scale, a feature which not only facilitated the construction of the diagrams but allows them to be readily extended beyond their present limits in any special case.

Diagram 5: As already stated, the discharge diagrams are based upon a friction factor n = .015. Diagram 5, consisting of four curves, representing different diameters, shows the relation between the discharge for n = .015 and discharges for other values of n, ranging from .008 to .018. For simplicity, this diagram may be considered a correction diagram on which the vertical scale represents friction factors and the horizontal scale correction coefficients to be applied to discharges for n = .015. The four curves intersect at a common point whose abscissa is 1.00 and ordinate .015, as might be expected. For diameters intermediate to those represented by the four curves interpolation will, of course, be necessary.

Diagrams 6—13: The remaining eight diagrams of the first group, termed for convenience ratio diagrams, give for each of the types of conduits considered the ratio of each of the three elements—area, mean velocity and discharge—of the "filled segment" to that of the "filled section" corresponding to any ratio of depth of flow to the vertical diameter. "Filled segment" refers to the cross section of the stream of the partially filled conduit, and "filled section" to the cross section of the entire conduit. The vertical scale represents the ratio of the depth of flow to the vertical diameter and the horizontal scale corresponding ratios of the hydraulic elements of the filled segment to those of the filled section.

Expressed also on each diagram are other hydraulic elements of the filled section in terms of the vertical or horizontal diameters; relations between the various geometrical elements for the purpose of outlining the section; and actual data from which the curves were constructed. These curves are strictly correct only for the data given, but they vary so slightly for different sizes, grades and friction factors that they may be considered practically independent of them.

The symbols and terms used on all ratio diagrams are those commonly employed in hydraulic work of this nature; the perimeter, P, the hydraulic radius, R, and area, A, referring, however, to the cross section of the entire conduit. The term "Equivalent" symbolized thus, = ==, when applied to the circle means one of equal carrying capacity and not of equal area.

In general these ratio diagrams represent types of sections commonly employed in practice, the different shapes of cross sections possessing either structural or hydraulic advantages. The circular section (Diag. 6) is the one most commonly employed in practice, combining strength with simplicity and economy of construction. The Gothic section (Diag. 7) combines the advantages of the circular section with increased strength of the Gothic arch. The catenary section (Diag. 9) is, theoretically, the section of greatest strength, but has the disadvantage of relatively low velocity for low flow. The egg-shaped section (Diag. 10), used somewhat extensively on combined systems of sewerage, has the hydraulic advantage of relatively high velocity for low flow. The horse shoe sections (Diagrams 12 and 13), used extensively for large-sized conduits, possess great stability with the additional advantage of economy in material and trench excavation. They have, however, the disadvantage of relatively low velocity for low flow. handle section (Diag. 8) is a modification of the horse shoe section in which the Gothic arch and rounded corners were intended to give greater stability. The square section (Diag. 11) is not common, but is occasionally used for wooden sewers and in other special cases; a little study will show its applicability to any rectangular section of moderate size which does not flow full.

The Gothic, basket handle and catenary sections have been used extensively on the Metropolitan sewers in Massachusetts; the horse shoe section (Diag. 12) on the Wachusett aqueduct, and the horse shoe section (Diag. 13) on the Croton aqueduct. The other sections are used more or less extensively in these and other localities.

#### Canals.

The four diagrams of the second group, though referring to water courses of a different hydraulic nature, are constructed upon lines closely analogous to those of the first group and will be compared closely with them.

With conduits, which are essentially closed channels, we have, for a full section of any type, a fixed relation between the various geometrical elements of the cross section, while with canals, in order to secure this fixed geometrical relation, we must assume a definite ratio between some of the elements. The length of base and depth of flow are chosen in the present instance, and a full section will here be assumed as one whose depth of flow is equal to one-half the base. That is, if a semicircle be described upon the base of a rectangular or trapezoidal section, a line drawn tangent to this semicircle and parallel with the base, will represent the flow line of a filled section. The ratio assumed is one which combines simplicity with economy of section, it being the theoretically economical ratio for rectangular sections and is the ratio from which no great variation might be expected in actual practice.

For similar sections, then, both the geometrical and hydraulic elements of filled sections become functions of the base, and consequently discharge and ratio diagrams may be constructed in which these elements are given in terms of the length of base, and the depth of filled section.

Diagram 14: This diagram gives, for rectangular filled sections, discharges in cubic feet per second, with corresponding velocities in feet per second, for lengths of base varying from 10 to 50 ft., hydraulic inclinations from 0.000004 to 0.001, and with a friction factor n = .025. The construction and appearance of this diagram is so similar to the four discharge diagrams for circular conduits that further description seems unnecessary.

Diagram 15: This diagram gives the relation between discharges from actual or equivalent rectangular filled section for n = .025 and discharges with other values of n ranging from .015 to .040. The diagram consists of three curves, and is similar in every way to Diagram 4 for conduits.

Diagrams 16 and 17: These two diagrams, termed ratio diagrams, are analagous to the eight ratio diagrams for conduits, and give for

canals the ratio of the two hydraulic elements—area and discharge—of the filled segment to that of the filled section corresponding to any ratio of depth of flow to depth of the filled section. These ratio diagrams differ from the previous ratio diagrams in that one of them, Diagram 16, refers exclusively to discharges, and the other, Diagram 17, exclusively to areas.

Since the ratio of the depth of flow to the length of base of a filled section is merely an assumed one, and, in reality, the section may flow at a relatively greater depth, the vertical scales on these two ratio diagrams are extended above the ratio 1.00 sufficiently to cover all cases which would probably arise in practice.

The table on Diagram 16 gives for trapezoidal filled sections, having various side slopes, the equivalent bases of rectangular filled sections of equal carrying capacity. A similar table on Diagram 17 gives simple equations for obtaining the area of trapezoidal filled sections directly in terms of the length of base. The mean velocity in all cases is obtained by dividing the discharge by the area.

#### CHAPTER III.

#### Use of the Diagrams.

In this chapter the following notation will be observed:

Qf, Vf, Af, and Df = Discharge, mean velocity, area and vertical diameter (or depth) of the full section:

 $Q_s$ ,  $V_s$ ,  $A_s$ , and  $D_s$  = Discharge, mean velocity, area and depth of the filled segment.

Qs Vs As Ds

-,-,-,= Ratios of the hydraulic elements of the filled Qf Vf Af Df segment to those of the filled section, expressed decimally.

H = horizontal diameter of conduit.

B = base of canal section.

Slopes = side slopes of trapezoidal canal section.

s = hydraulic slope or sine of angle of inclination.

n = friction factor dependent upon character of internal surface.

#### Conduits.

Conduits may flow full, partially full or under pressure. They are usually designed to carry a uniform flow under the varying conditions of Q (or V), D, s and n. Three of these conditions are usually given or assumed, and the remaining one may be obtained by the use of the diagrams. The following rules, classified under the three conditions of flow, will illustrate the proper method of using the diagrams and will serve as a special guide in practice.

#### Class A.—Conduits flowing full.

When the section is circular the following principal cases (1-4) may occur:

(1) Given Df, s and n, to obtain Qf. With Df and s find Qf for n = .015 from Diagram 1, 2, 3 or 4. The product of this Qf and the ratio on Diagram 5 corresponding to given value of n will give required Qf.

(2) Given  $Q_f$ , s and n to obtain D: Divide  $Q_f$  by ratio on Diagam 5 corresponding to given n. With this  $Q_f$  corresponding to n = .015, and given s, find required  $D_f$  from Diagrams 1, 2, 3 or 4. This case is slightly tentative, since  $D_f$  is required in the use of Diagram 5. It will be seen, however, that ratios on diagram 5 corresponding to any friction factor, n, vary but slightly for a wide range in values of D, so that a value of D sufficiently accurate to use Diagram 5 may be first made by inspection.

(3) Given  $Q_f$ ,  $D_f$  and n to obtain s: Divide given  $Q_f$  by ratio on Diagram 5 corresponding to given n. With this  $Q_f$  corresponding to n = .015, and given  $D_f$ , find required s from Diagrams 1, 2, 3 or 4.

(4) Given  $Q_f$  (obtained from direct observation),  $D_f$  and s to obtain n: With given  $D_f$  and s find  $Q_f$  from Diagrams 1, 2, 3 or 4 for n = .015. Divide observed  $Q_f$  by  $Q_f$  for n = .015, and with this ratio find required n from Diagram 5.

In the above four cases V<sub>f</sub> may be substituted for Q<sub>f</sub>, since Diagrams 1, 2, 3 and 4 give V<sub>f</sub> corresponding to Q<sub>f</sub> and since for any diameter, V<sub>f</sub> varies directly as Q<sub>f</sub>. A<sub>f</sub> in these cases is obtained geometrically from D<sub>f</sub>.

In the next four cases, in which the section is not circular, as for instance the Gothic, egg-shaped and horse shoe, a comparison is



necessary between the vertical diameters of these sections, and the diameters of circular sections of equal carrying capacity.

The equations for this comparison are given on each of the ratio diagrams, as are also the geometrical relations, in terms of the vertical or horizontal diameter, necessary to outline the section. The Gothic section will be chosen as an example of these different types of sections and the rules given above when applied to this section become as follows:

- (5) Given  $D_f$ , s and n of a Gothic section to obtain  $Q_f$ : From Diagram 7, Diam. of  $= \bigcirc = \text{circle} = \frac{D_f}{1.1056}$ . With this Diam. and given s find  $Q_f$  for n = .015 from Diagrams 1, 2, 3 or 4. The product of this  $Q_f$  and the ratio on Diagram 5 corresponding to given n, will give required  $Q_f$ .
- (6) Given Qf, s and n of a Gothic section to obtain Df and outline the section. With given Qf, s and n obtain Df of a circular section by (A-2). With this Df obtain, from Diagram 7, required Df of Gothic section by equation Vert. Diam. = 1.1056 × Diam. of = □ = circle. With Df thus found outline section from relation of geometrical elements on Diag. 7.
- (7) Given  $D_f$ , n and  $Q_f$  of a Gothic section to obtain s. By Diagram 7, Diam. of  $= \bigcirc = \text{circle} = \frac{D_f}{1.1056}$ . Divide given  $Q_f$  by ratio on Diagram 5, corresponding to given n. With this  $Q_f$  corresponding to n = .015, and Diam. of  $= \bigcirc = \text{circle}$ , obtain required s from diagrams 1, 2, 3 or 4.
- (8) Given Df, s and Qf (obtained from direct observation) of a Gothic section to obtain n. From Diag. 7, Diam. of  $= \bigcirc =$  circle  $= \frac{D_f}{1.1056}$ . With this Diam. and given s find Qf for n = .015 from Diagrams 1, 2, 3 or 4. Divide observed Qf by Qf for n = .015 and with this ratio find required n from Diagram 5.

In the last four cases  $A_f$  is obtained from  $D_f$  by equations given on the ratio diagrams, and  $V_f$  by dividing  $Q_f$  by  $A_f$ . Also since the Diam. of  $= \bigcirc =$  circle refers to equal capacity and not equal area, in general  $V_f$  cannot be substituted for  $Q_f$  as in the first four cases.

#### Class B.—Conduits flowing partially full.

Cases arising in this class involve merely an extended use of the ratio diagrams, and the principles involved above. To avoid confusion the Gothic section will be retained as an example in the following cases of this class.

- (1) Given  $D_f$ ,  $D_s$  and  $Q_f$  or  $V_f$  or  $A_f$  of a Gothic section to obtain  $Q_s$ ,  $V_s$  and  $A_s$ . From Diagram 7 obtain  $\frac{Q_s}{Q_f}$ ,  $\frac{V_s}{V_f}$  and  $\frac{A_s}{A_f}$  corresponding to  $\frac{D_s}{D_f}$ . The product of  $Q_f$  and  $\frac{Q_s}{Q_f}$  will give required  $Q_s$ ; product of  $V_f$  and  $\frac{V_s}{V_f}$  required  $V_s$ ; product of  $A_f$  and  $\frac{A_s}{A_f}$  required  $A_s$ .
- (2) Given  $D_f$ ,  $D_s$  and  $Q_s$  or  $V_s$  or  $A_s$  of a Gothic section to obtain  $Q_f$ ,  $V_f$  and  $A_f$ . From Diagram 7 obtain  $\frac{Q_s}{Q_f}$ ,  $\frac{V_s}{V_f}$  and  $\frac{A_s}{A_f}$  corresponding to  $\frac{D_s}{D_f}$ . The quotient of  $Q_s$  by  $\frac{Q_s}{Q_f}$  will give required  $Q_f$ ; quo-

tient of  $V_s$  by  $\frac{V_s}{V_f}$  required  $V_f$ ; quotient of  $A_s$  by  $\frac{A_s}{A_f}$  required  $A_f$ .

- (3) Given s, n, D<sub>s</sub> and D<sub>f</sub> of a Gothic section to obtain Q<sub>s</sub>. With given D<sub>f</sub>, s and n obtain Q<sub>f</sub> by (A-5). With this Q<sub>f</sub> and given D<sub>s</sub> and D<sub>f</sub> obtain Q<sub>s</sub> by (B-1).
- (4) Given  $Q_8$ , n,  $D_8$  and  $D_f$  of a Gothic section to obtain s. With given  $Q_8$ ,  $D_8$  and  $D_f$  obtain  $Q_f$  by (B-2). With  $Q_f$ , and given n and  $D_f$  obtain required s by (A-7).
- (5) Given Q<sub>8</sub> (obtained from direct observation), s, D<sub>8</sub> and D<sub>f</sub> of a Gothic section to obtain n. With given D<sub>f</sub>, D<sub>8</sub> and Q<sub>8</sub> obtain Q<sub>f</sub> by (B-2). With this Q<sub>f</sub> and given D<sub>f</sub> and s find required n from (A-8).
- (6) Given  $Q_8$ , s, n and  $D_f$  of a Gothic section to obtain  $D_8$ . With given s, n and  $D_f$  obtain  $Q_f$  by (A-5). The product of  $D_f$  and  $\frac{D_8}{D_f}$  corresponding to  $\frac{Q_8}{Q_f}$  will give required  $D_8$ .

- (7) Given Q<sub>8</sub>, s, n and D<sub>8</sub> of a Gothic section to obtain D<sub>f</sub>. A tentative method is necessary as follows: Assume D<sub>f</sub>, and, with given s and n and D<sub>8</sub>, obtain a trial Q<sub>8</sub> by (B-3), which should agree with given Q<sub>8</sub> if D<sub>f</sub> is correctly assumed; if not, assume new values of D<sub>f</sub> until the proper one is found.
  - (8) Given  $\frac{D_s}{D_f}$  (but knowing neither  $D_s$  nor  $D_f$ ),  $Q_s$ , s and n of

a Gothic section to obtain  $D_f$ . Obtain  $Q_f$  from  $Q_s$  and  $\frac{D_s}{D_f}$  by (B-2), and with this  $Q_f$  and given s and n obtain  $D_f$  by (A-6).

Class C.—Conduits under Pressure.

With conduits flowing under pressure, the following losses of head are usually considered: Loss due to generating velocity, loss due to entrance, loss due to internal friction, and loss due to special causes, such as valves and sudden bends.

For uniform flow in long conduits the losses due to entrance and to generating velocity are relatively small and for entrance similar to a standard short tube, these two losses combined amount ap-

proximately to 1.5—. Losses due to valves and bends, also

usually small, and requiring special treatment, will not be considered here.

The principal loss, then, and the only one which is considered here, is that due to internal friction, and usually represented by the hydraulic gradient—or the line joining water levels in piezometers placed at points along the conduit and which for convenience, will here be assumed as straight.

If the conduit does not at any point rise above this hydraulic gradient, and if we let s represent the inclination of this hydraulic gradient, the solution of cases in this class will be the same as for cases under Class A, to which the reader is referred.

#### Canals.

Under the present treatment of canals in which the "Filled Section" is an assumed one having a depth equal to one-half the base, only two conditions of flow have a practical significance: Flow in which the ratio of depth of flow to depth of filled section is 1.00 (i. e.

flowing full), and flow in which this ratio is greater or less than 1.00. The two classes corresponding to these two conditions will be considered separately.

Class A.—Sections in which the ratio of depth of flow to depth of "Filled Section" is 1.00.

If the sections are rectangular the following four principal cases occur:

- (1) Given B, s and n to obtain  $Q_f$ . With given B and s obtain  $Q_f$  for n = .025 from Diagram 14. The product of this  $Q_f$  and the ratio from Diagram 15 corresponding to given n will give required  $Q_f$ .
- (2) Given  $Q_f$ , s and n to obtain B. Divide  $Q_f$  by ratio on Diagram 15 corresponding to given n and with this  $Q_f$ , corresponding to n = .025, and given s, find required B from Diagram 14. This case is also slightly tentative as in the case of conduits (A-2) and an estimate of B is necessary in advance in order to use Diagram 15.
- (3) Given  $Q_f$ . B, and n to obtain s. Divide given  $Q_f$  by ratio on Diagram 15 corresponding to given n. With this  $Q_f$  for n = .025 and given B find required s from Diagram 14.
- (4) Given  $Q_f$  (obtained from direct observation), B and s to obtain n. With given B and s obtain  $Q_f$  for n=.025 from Diagram 14. Divide observed  $Q_f$  by  $Q_f$  for n=.025 and with this ratio find required n from Diagram 15.

In the above four cases V<sub>f</sub> may be substituted for Q<sub>f</sub> for reasons similar to those previously described under Class A, for conduits, A<sub>f</sub> in all cases is obtained from equations on Diagram 17.

If the sections are trapezoidal these four cases are modified, and the section with side slopes of 2 to 1 will be considered an example. as follows:

- (5) Given B, s and n of a trapezoidal section having side slopes of 2 to 1, to obtain Q<sub>f</sub>. From Diagram 16 base of = = Rect. section
- $=\frac{\mathrm{B}}{0.73}$ . With this base and given s find Qf for n = .025 by Dia-
- gram 14. The product of this  $Q_f$  and the ratio on Diagram 15 corresponding to given n will give required  $Q_f$ .
- (6) Given Q<sub>f</sub>, s and n of a trapezoidal section having side slopes of 2 to 1 to obtain B. With given Q<sub>f</sub>, s and n obtain B of rectangular section by (A-2). From Diagram 16, required B = .73 × Base of = ⊃= Rect. Section.

(7) Given  $Q_f$ , B and n of a trapezoidal section with slopes of 2 to 1 to obtain s. From Diagram 16 Base of = Rect. Section =  $\frac{B}{0.73}$ . Also, divide given  $Q_f$  by ratio on Diagram 15 corresponding to given n. With this  $Q_f$  for n = .025 and Base = Rect. Section obtain required s from Diagram 14.

(8) Given  $Q_f$  (obtained from direct observation), B and s of a trapezoidal section with side slopes of 2 to 1 to obtain n. From Diagram 16, Base of = = Rect. Section =  $\frac{B}{0.73}$ . With this Base and given s find  $Q_f$  for n = .025 from Diagram 14. Divide observed  $Q_f$  by  $Q_f$  for n = .025, and with this ratio find required n from Diagram 15.

In the last four cases V<sub>f</sub> cannot, in general, be substituted for Q<sub>f</sub> for reasons similar to those previously given under Class A for conduits. A<sub>f</sub> in all cases is obtained from equations on Diagram 17, and V<sub>f</sub> by dividing Q<sub>f</sub> by A<sub>f</sub>.

Class B.—Sections in which the ratio of depth of flow to depth of

"Filled Section" is greater or less than 1.00.

(1) Given  $D_f$  (or, if B is given,  $D_f = \frac{1}{2}$  B),  $D_s$  and  $Q_f$  or  $A_f$  of a trapezoidal section with side slopes of 2 to 1, to obtain  $Q_s$  and  $A_s$ . From Diagrams 16 and 17 obtain  $\frac{Q_s}{Q_f}$  and  $\frac{A_s}{A_f}$  corresponding to  $\frac{D_s}{D_f}$ .

The product of  $Q_f$  and  $\frac{Q_s}{Q_f}$  will give required  $Q_s$ ; the product of  $A_f$ 

and  $\frac{A_s}{A_f}$  required  $A_s$ . In all cases where  $V_f$  and  $V_s$  are sought they are obtained by dividing  $Q_f$  by  $A_f$  or  $Q_s$  by  $A_s$ , respectively.

(2) Given  $D_f$ ,  $D_s$  and  $Q_s$  or  $A_s$  of a trapezoidal section with side slopes of 2 to 1 to obtain  $Q_f$  and  $A_f$ . From Diagrams 16 and 17 obtain  $\frac{Q_s}{Q_f}$  and  $\frac{A_s}{A_f}$  corresponding to  $\frac{D_s}{D_f}$ . The quotient of  $Q_s$  by  $\frac{Q_s}{Q_f}$  will give required  $Q_f$ ; quotient of  $A_s$  by  $\frac{A_s}{A_f}$  required  $A_f$ .  $V_s$  and  $V_f$  are obtained by division as before.

(3) Given s, n, D<sub>s</sub> and B (or D<sub>f</sub> which equals ½ B) of a trapezoidal section with side slopes of 2 to 1 to obtain Q<sub>s</sub>. With given B, s and

With this Qf and given Ds and Df obtain n obtain  $Q_f$  by (A-5). required Q<sub>s</sub> by (B-1).

- (4) Given Qs, n, Ds and B of a trapezoidal section with side slopes of 2 to 1 to obtain s. From Ds, B and Qs obtain Qf by (B-2). With Qf and given n and B obtain required s by (A-7).
- (5) Given Q<sub>s</sub> (obtained from direct observation), s, D<sub>s</sub> and B of a trapezoidal section with side slopes of 2 to 1 to obtain n. With given Qs, B and Ds obtain Qf by (B-2). With this Qf and given B and s find required n from (A-8).
- (6) Given Qs, s, n and B of trapezoidal section with side slopes of 2 to 1 to obtain Ds. With given s, n and B obtain Qf by (A-5).

With  $\frac{Q_s}{Q_f}$  find  $\frac{D_s}{D_f}$  from Diagram 16. The product of  $D_f$  (equal to

- $\frac{1}{2}$  B) and  $\frac{D_8}{D_6}$  gives required  $D_8$ .
- (7) Given Q<sub>8</sub>, s, n and D<sub>8</sub> of a trapezoidal section with side slopes of 2 to 1 to obtain B. A tentative method is necessary. Assume B, and, with given s, n and Ds, obtain a trial Qs by (B-3), which should agrèe with given  $Q_s$  if B is correctly assumed; if not assume new values of B until the proper one is found.
- (8) Given  $\frac{D_s}{D_f}$  or  $\frac{D_s}{B}$  (but knowing neither  $D_s$ ,  $D_f$  nor B),  $Q_s$ ,  $S_s$ and n of a trapezoidal section with side slopes of 2 to 1 to obtain B.

With given  $Q_s$  and  $\frac{D_s}{D_f}$  or  $\frac{D_s}{B}$  obtain  $Q_f$  by (B-2). With  $Q_f$  and given s and n obtain B by (A-6).

The following two numerical examples will now be given which may further illustrate the use of the diagrams of the two groups.

(Ex. 1). Let it be required to find the hydraulic slope of an eggshaped conduit 24 × 36 ins., which, when flowing 1.5 ft. deep will discharge 4 cu. ft. per sec. with n = .014. The case falls under (B-4) for conduits in which  $Q_s = 4$ , n = .014,  $D_s = 18$  ins.,  $D_f = 36$  ins.

and required to obtain s.  $\frac{D_s}{D_f} = \frac{18}{36} = .500$ . By Diagram 10,  $\frac{Q_s}{Q_f} = \frac{18}{100}$ 

0.425. Also Diam. of = = circle =  $\frac{36}{1.254}$  =  $28\frac{1}{2}$  ins. Qf =

 $\frac{4.0}{0.425}$  = 9.41 cu. ft. per sec.  $Q_f$  (for n = .015) =  $\frac{9.41}{1.09}$  = 8.6 cu. ft. per sec. (by Diagram 5), which, with diameter  $28\frac{1}{2}$  ins., gives required s = 0.0008 = 1 in 1250 by Diagram 3.

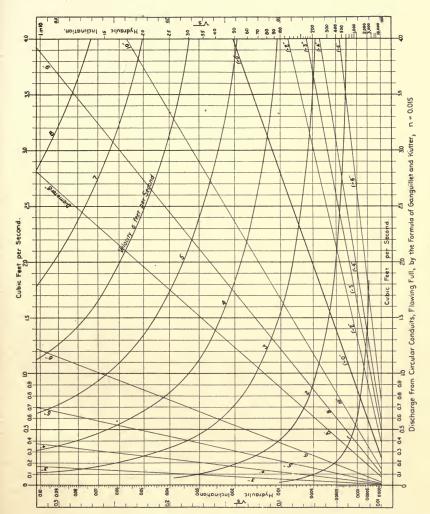
(Ex. 2). Let it be required to find the discharge of a trapezoidal canal with length of base 18 ft., side slopes 1 to 1, flowing 8 ft. deep, with s = 1 in 5,000, and n = .020. The case falls under (B-3) for Canals. For the filled section, then, B = 18 ft., and D = 9 ft.

By Diagram 16, Base of = = Rect. section =  $\frac{18}{0.80}$  = 22.5 ft., which, with given s = 1 in 5,000, gives  $Q_f = 683$  cu. ft. per sec. for n = .025 (by Diagram 14).  $Q_f$  (for n = .020) =  $683 \times 1.235$  = 843 cu. ft. per sec. by Diagram 15.  $\frac{D_s}{D_f} = \frac{8}{9} = 0.889$ , which, for

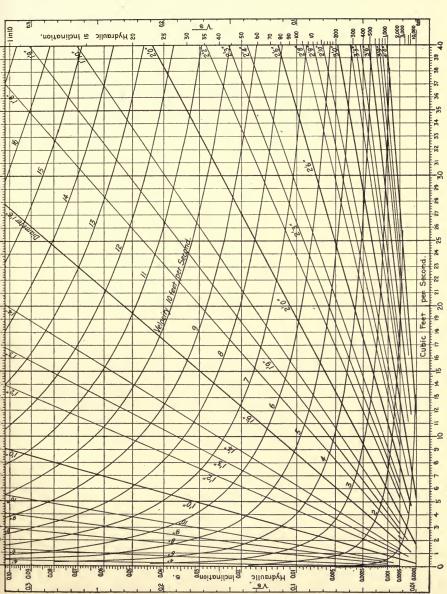
side slopes 1 to 1 gives  $\frac{Q_s}{Q_f}$  = 0.81 (by Diagram 16). Required  $Q_s$  = 843 × 0.81 = 683 cu. ft. per sec.

In conclusion, it may be said as to the accuracy of using these diagrams that, disregarding personal errors in reading, there will be a slight disagreement between results computed by the general formula and those given by the diagrams, due to the nature of the formula and the method of constructing the diagrams; that this disagreement will be greater for canals than for conduits, owing to the greater range of data considered under canals; and that for ordinary practice this disagreement should not be greater than one or two per cent. for conduits and two or three per cent. for canals.

Disagreements in this amount have little importance, however, when we consider that first the formula itself is empirical and, being based largely upon experiments, is subject to necessary errors in its deduction; also, that the uncertainties in selecting values for n are appreciable, and are greater for canals than for conduits, as will be seen from a study of the classified values of n in conjunction with Diagrams 5 and 15.

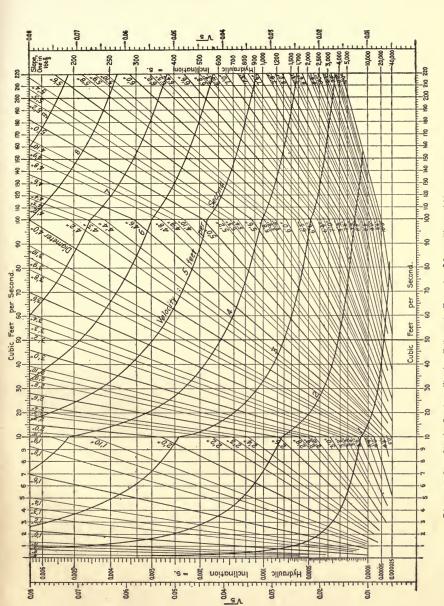






Discharge from Circular Conduits, Flowing Full, by the Formula of Ganguillet and Kutter, n = 0.015





Discharge from Circular Conduits, Flowing Full, by the Formula of Ganguillet and Kutter, n= 0.015 DIAGRAM 3.



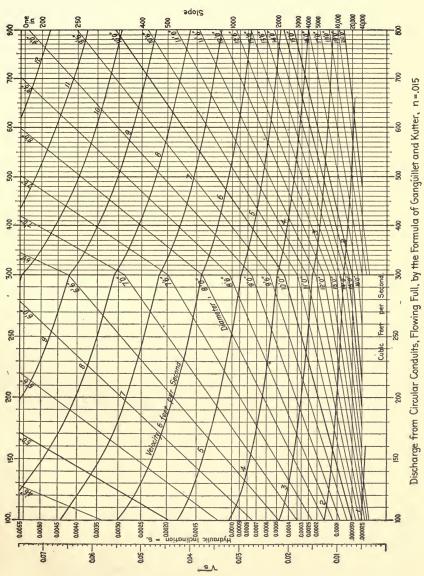
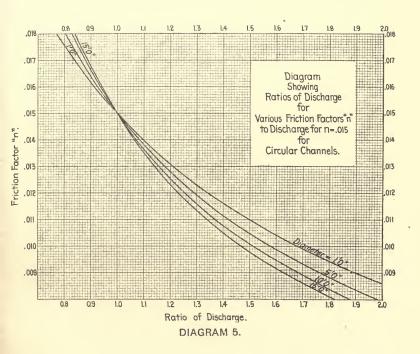
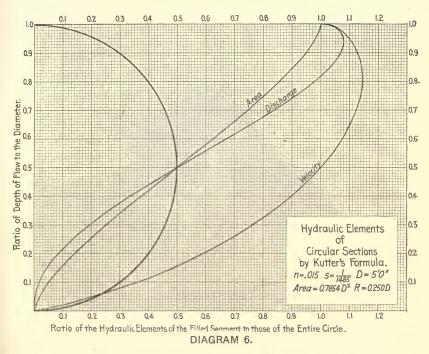


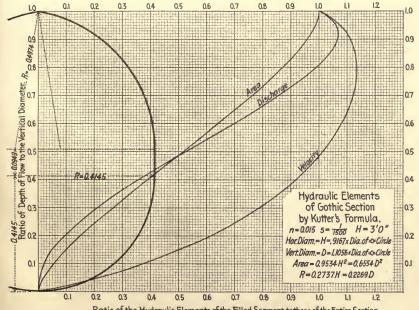
DIAGRAM 4.







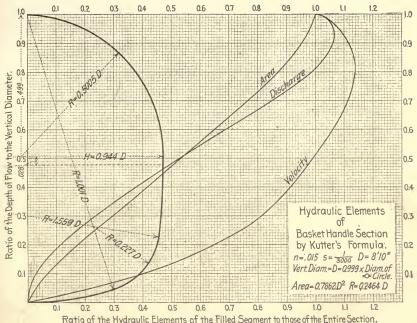




Ratio of the Hydraulic Elements of the Filled Segment to those of the Entire Section.

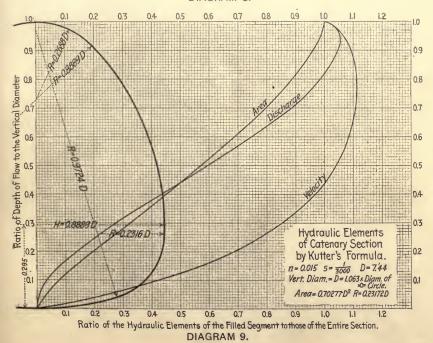
DIAGRAM 7.



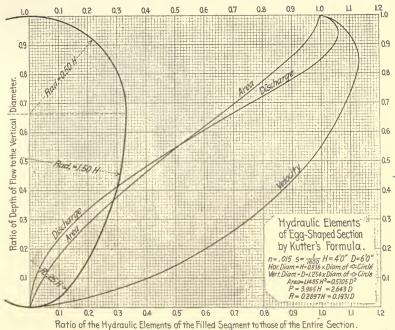


Ratio of the Hydraulic Elements of the Filled Segment to those of the Entire Section.

## DIAGRAM 8.









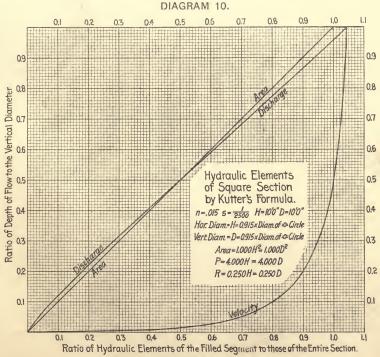
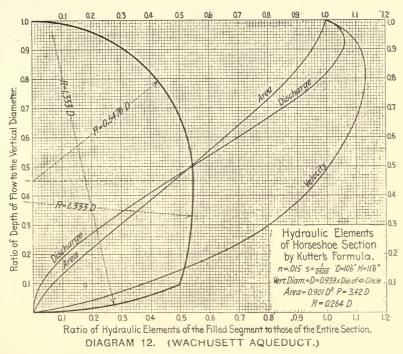
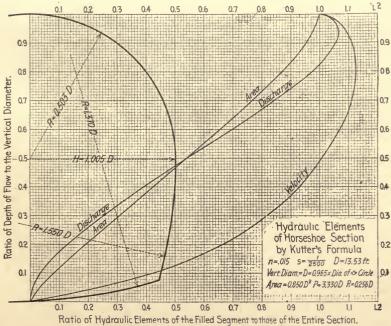


DIAGRAM 11.



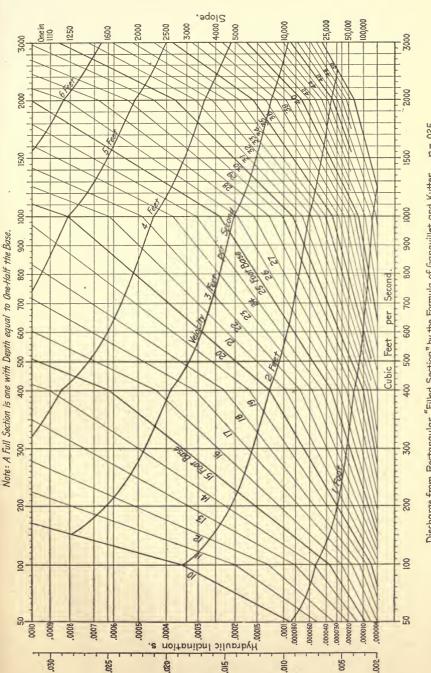




(CROTON AQUEDUCT.)

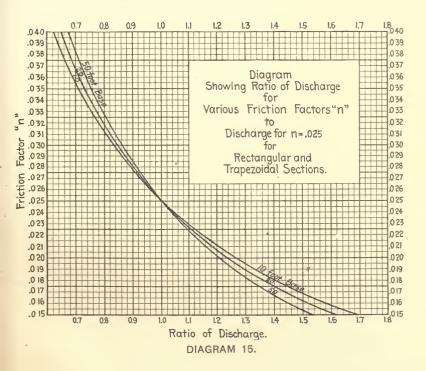
DIAGRAM 13.



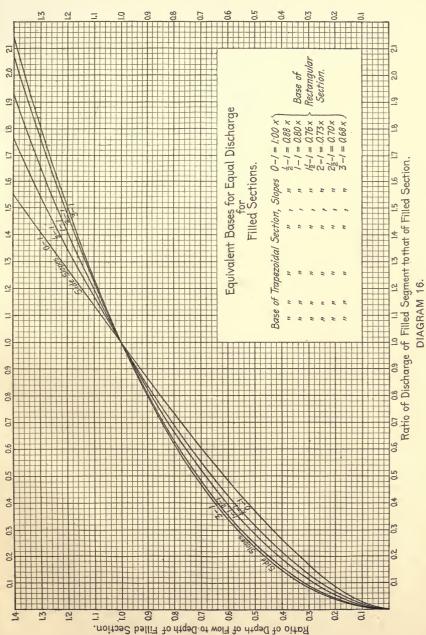


Discharge from Rectangular "Filled Section" by the Formula of Ganguillet and Kutter DIAGRAM 14.

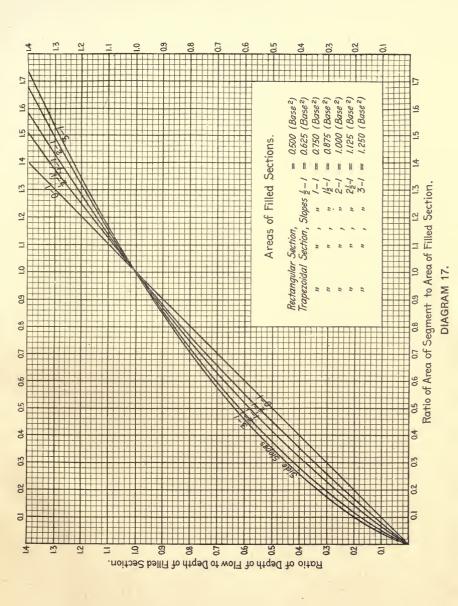
















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